

1) Let $f$ and $g$ be functions given by $f(x)=\frac{1}{4}+\sin (\pi x)$ and $g(x)=4^{-x}$. Let $R$ be the shaded region in the first quadrant enclosed by the $y$-axis and the graphs of $f$ and $g$, and let $S$ be the shaded region in the first quadrant enclosed by the graphs of $f$ and $g$, as shown in the figure above.
a) Find the area of $R$.
b) Find the area of $S$.
c) Find the volume of the solid generated when $S$ is revolved around the horizontal line $y=-1$.
